

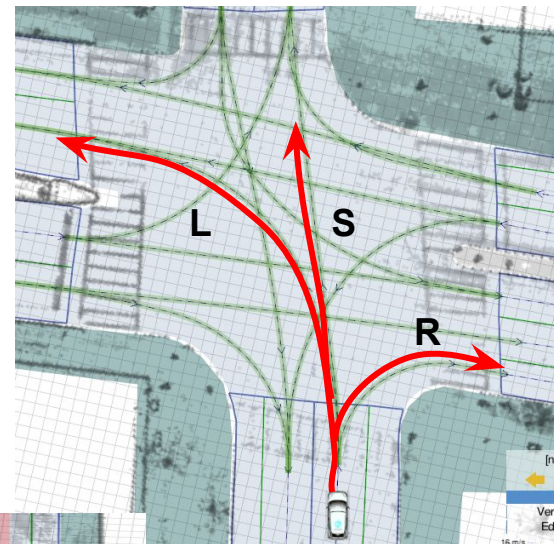
MIXTURE OF EXPERTS MODEL FOR TRAJECTORY PREDICTION

PULKIT KATDARE

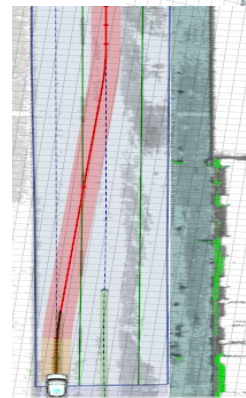
15 AUGUST, 2019

PREDICTION TEAM

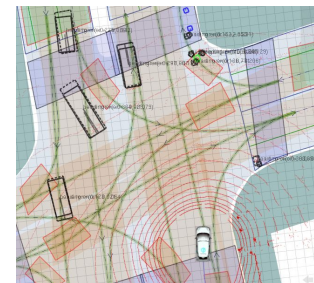
- Model possible future states of the world
- Planner uses to enable safe and natural driving by better anticipating interactions with others
- Flexible models support different behaviors in multiple cities/countries (Boston, SG, Vegas)



Lane Target Prediction



Lane Changing

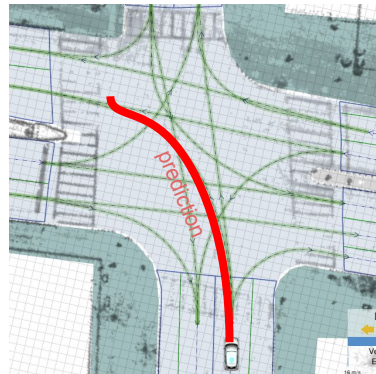


Pass/yield behavior

OVERVIEW

- We use different kind of models based on
 - Physics
 - Micro-planners
 - Machine learning
- Each of these models are generally well-suited for different kinds of motion
- Can we leverage these models to hopefully improve our results?

TRAJECTORY PREDICTION MODEL



TOWARDS MULTIPLE PREDICTIONS

- Impossible to predict exact trajectories for vehicles
- Is it possible to leverage the models in our repository along with their probability to improve prediction
- Could help planning team develop risk-aware algorithms



RELATED WORK

1. Multimodal Trajectory Predictions for Autonomous Driving using Deep Convolutional Networks (Cui et al.)
2. Adaptive Mixture of Local Experts (Jacobs et al.)

- [1]: FCN for multi-modal prediction
- [2]: Mixture of Expert based architecture

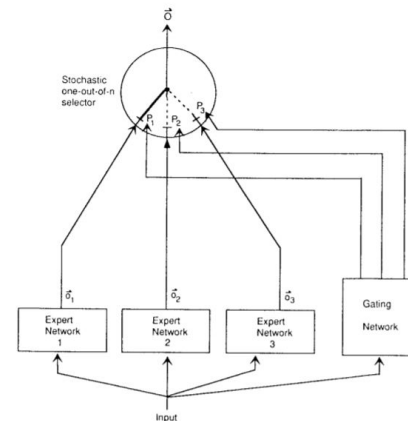
$$m^* = \arg \min_{m \in \{1, \dots, M\}} \text{dist}(\tau_{ij}, \tilde{\tau}_{imj}). \quad (3)$$

$$\mathcal{L}_{ij}^{\text{class}} = - \sum_{m=1}^M I_{m=m^*} \log p_{im}, \quad (5)$$

Probability For the mth mode

Ground Truth For jth mode

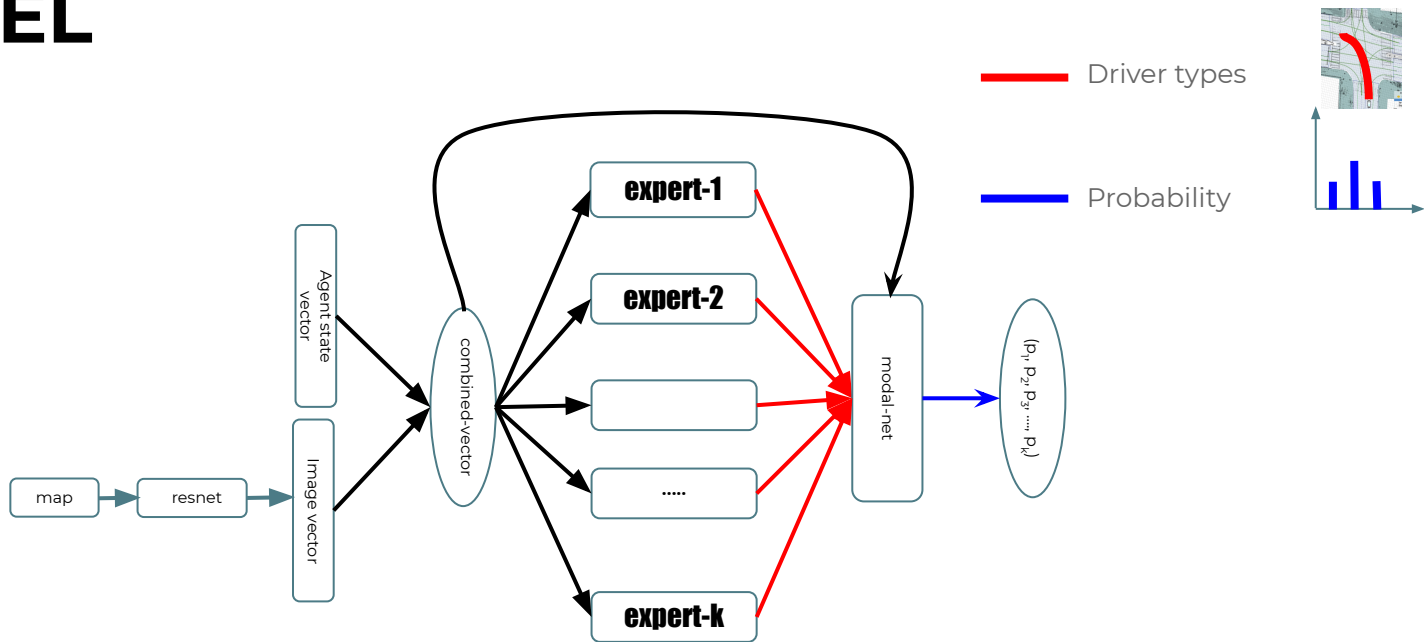
Predicted Trajectory for mth mode



APPROACHES

1. **END-TO-END MIXTURE-OF-EXPERTS MODEL**
2. **FROZEN MOE MODEL**

END-TO-END MIXTURE-OF-EXPERTS (MOE) MODEL



END-TO-END MODEL

$$\mathcal{L}(Z, \tau) = \sum_{i=1}^k p_i L(E_k(Z), \tilde{\tau})$$

Z: input to the network

τ : ground truth

$E_k(\cdot)$: output by a specific expert- k

1. Adaptive Mixture of Local Experts (Jacobs et al.)

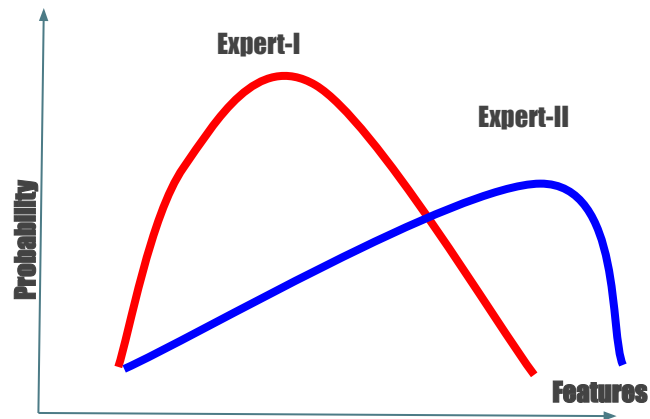
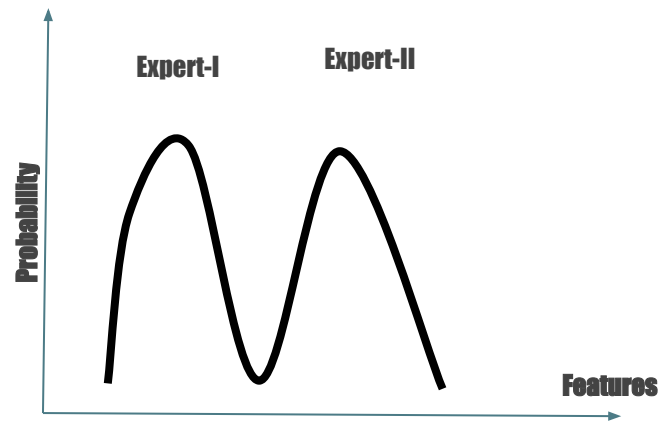
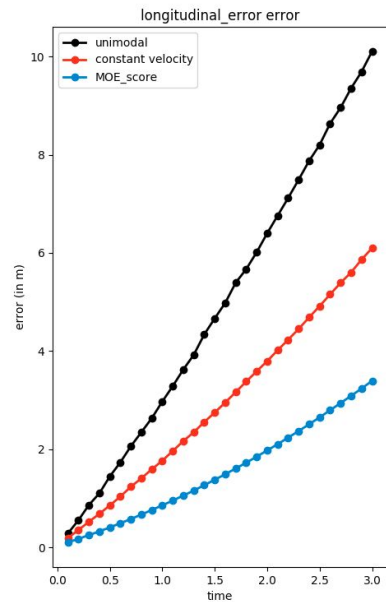
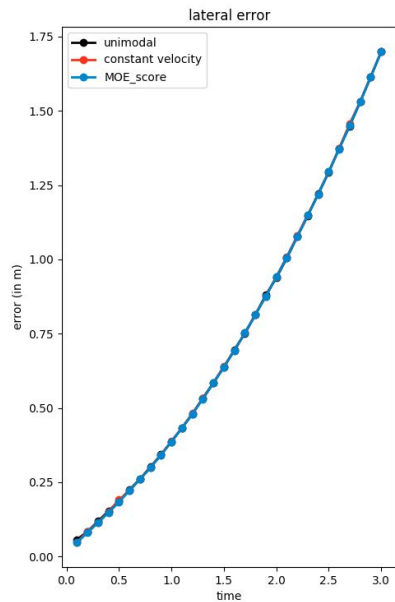
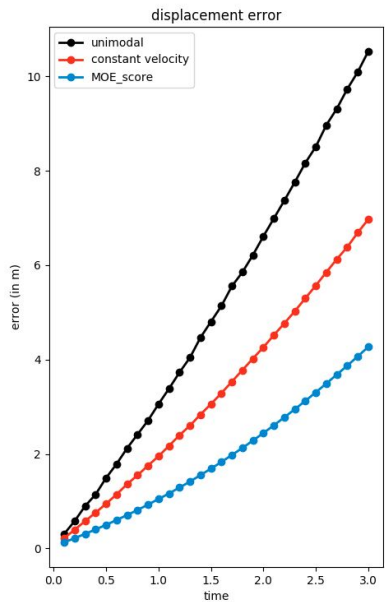
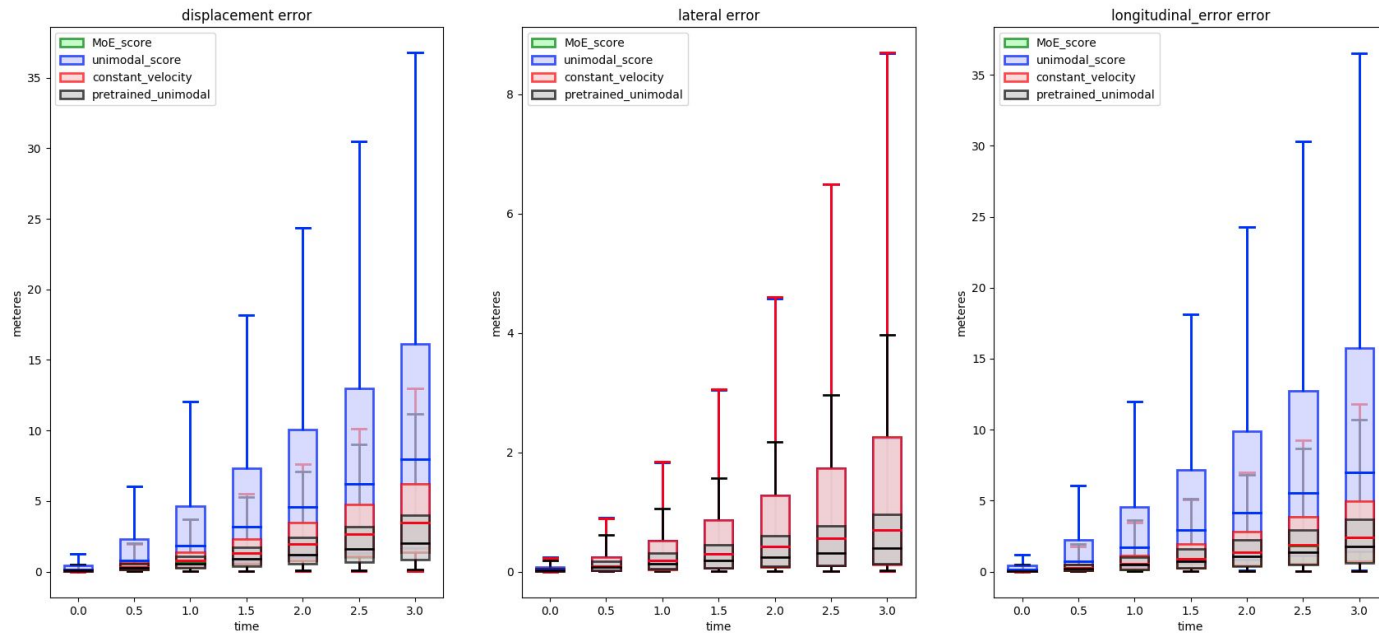


Illustration of Mode Collapse

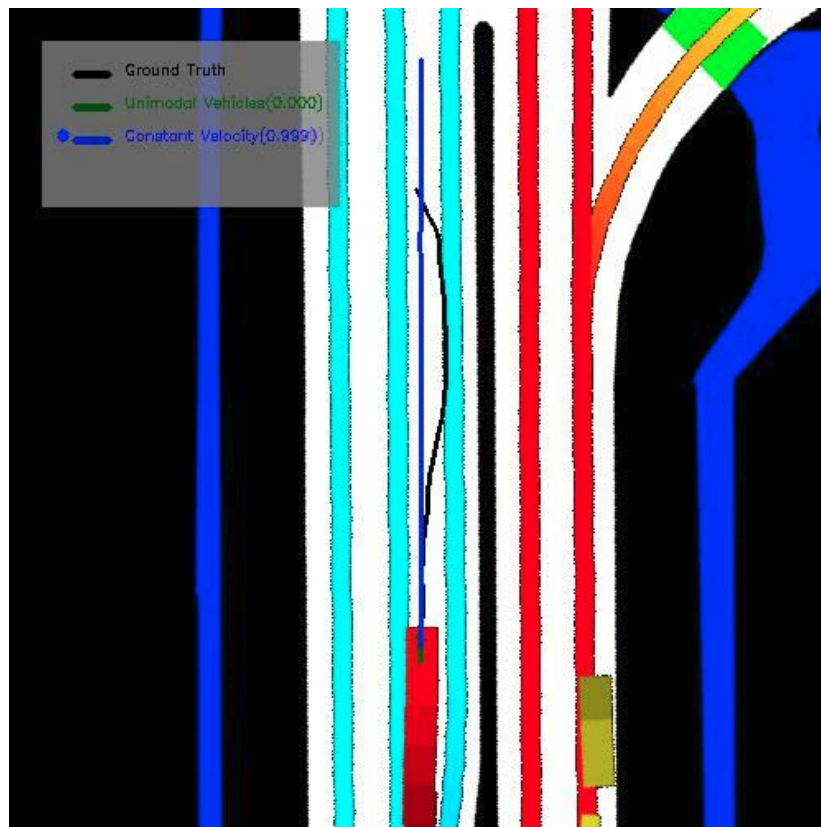
EXPERTS: CONSTANT VELOCITY, VEHICLES (TRAIN TRACKS: 300K VEHICLES)



EXPERTS: CONSTANT VELOCITY, VEHICLES (TRAIN TRACKS: 300K VEHICLES)



RESULTS

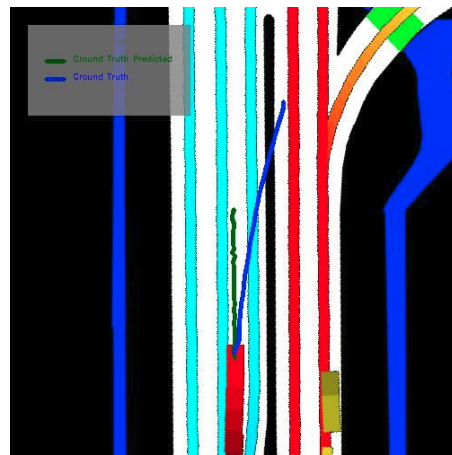
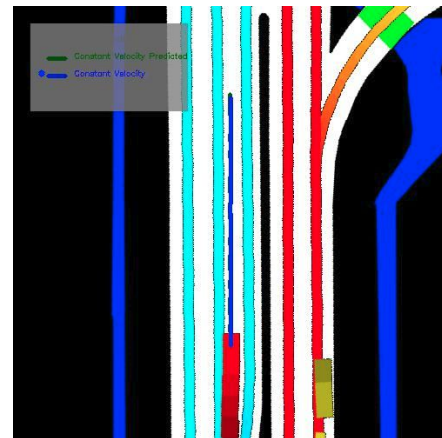


RESULTS

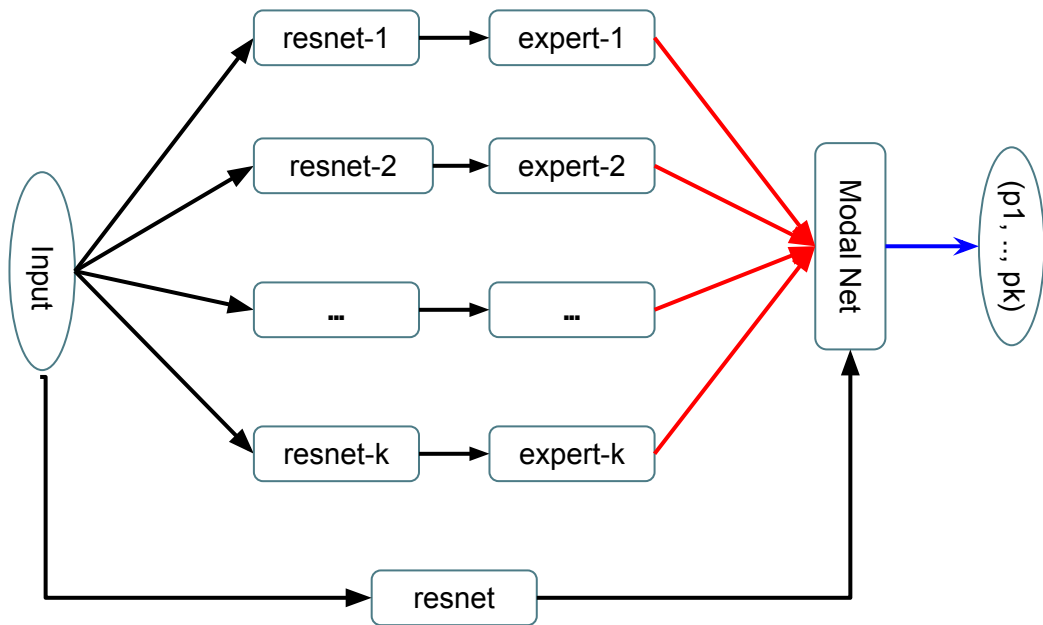


CONCLUSION

- Individual experts perform worse than the unimodal ones
- Mode collapse
 - Constant velocity is the dominant prediction
 - Model complexity of two models are different
- Leverage existing models to learn a probability distributions over driver types

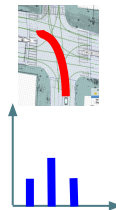


FROZEN MOE MODEL

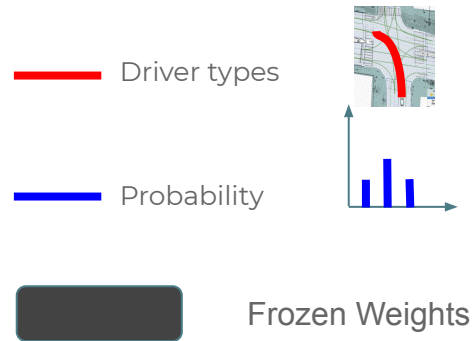
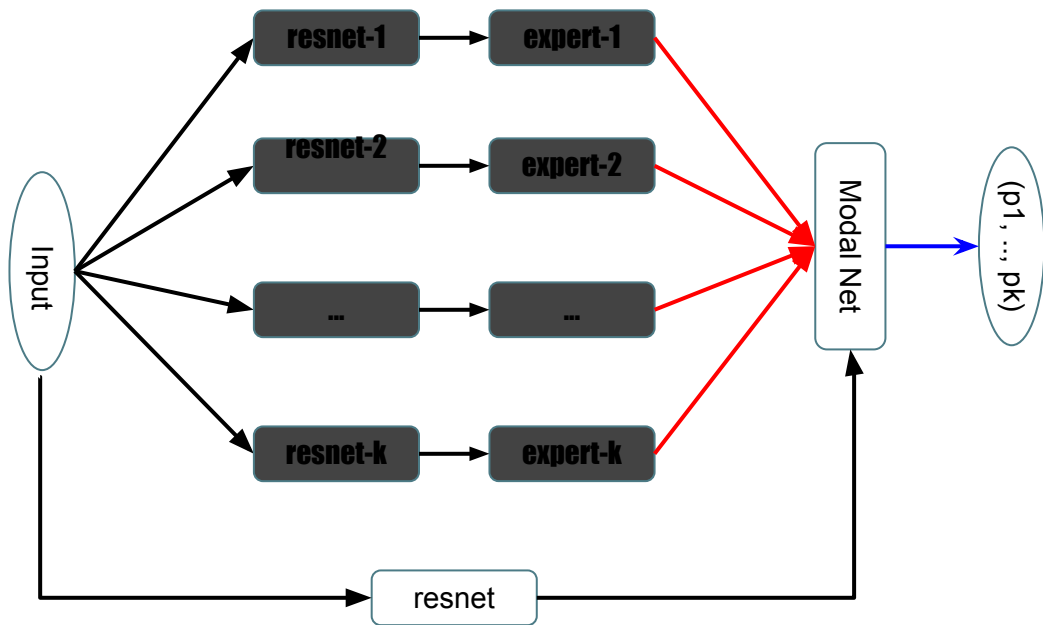


— Driver types

— Probability



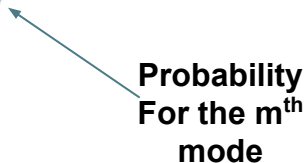
FROZEN MOE MODEL



TRAINING THE DISCRIMINATOR

- Proposes a loss function just for discriminator training [1]

$$k^* = \arg \min_{i \in \{1, 2, \dots, k\}} \text{dist}(\tau_{ij}, \tilde{\tau}_j) \longrightarrow \text{Ground Truth}$$

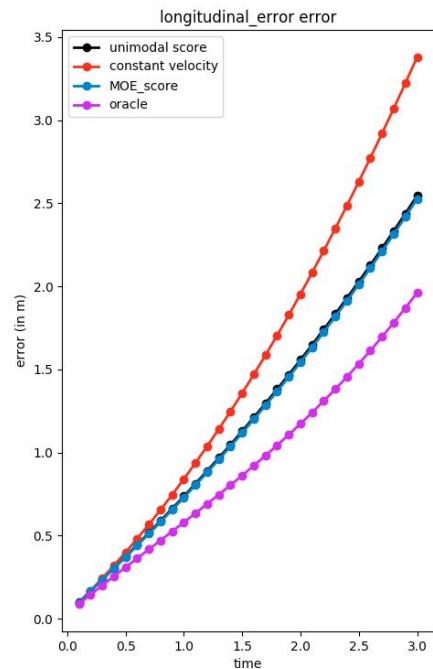
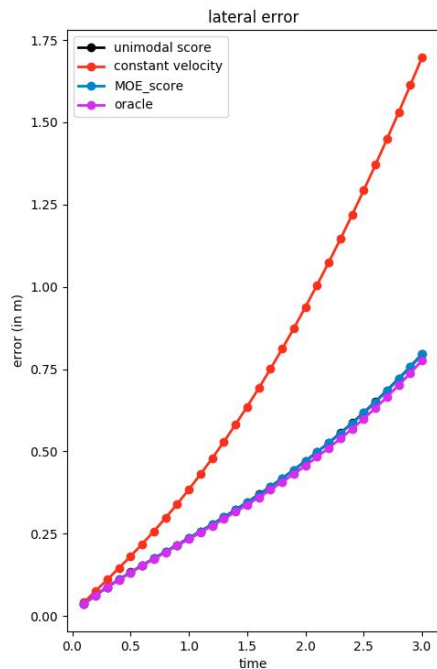
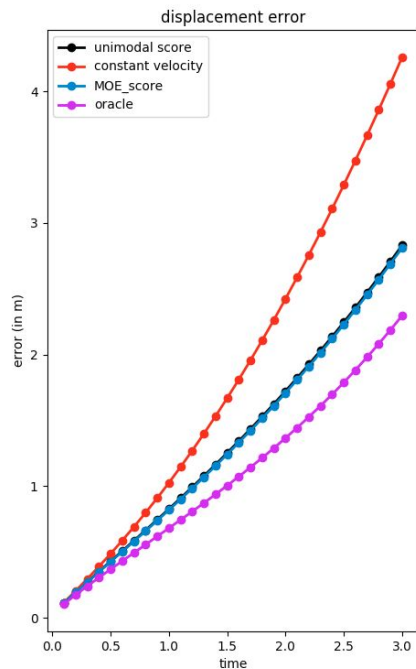

$$\mathcal{L}_{ij}^{class} = - \sum_{i \in \{1, 2, \dots, k\}} I_{i=i^*} \log(p_{im})$$


- In our particular case, the dist function is a smooth L1-norm

EXPERIMENTS

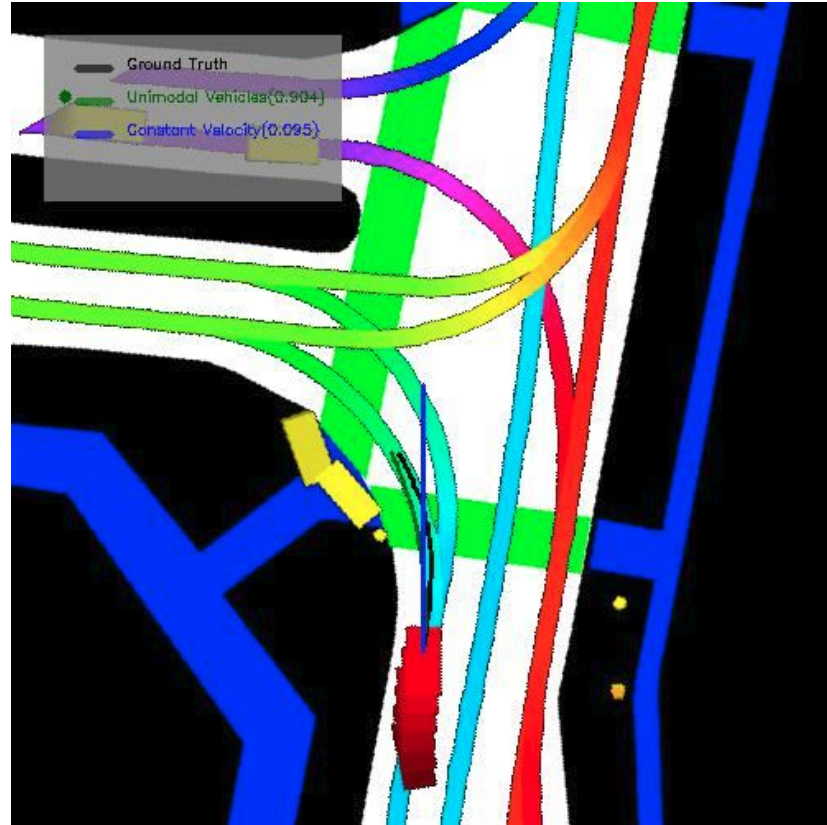
1. Experts: Constant Velocity, Unimodal
Train Tracks: 300K, 3 Million
Training Data: **Vehicle Tracks**
2. Experts: Vehicles, Pedestrian, Cyclists, Constant Velocity
Train Tracks: 600k, 3 Million, 5 Million
Training Data: **Vehicle, Pedestrian and Cyclists Tracks**
3. Experts: Pedestrians, Vehicles, Unclassified
Train Tracks: 6 Million
Training Data: **Pedestrians, Vehicles, Unclassified Tracks**

EXPERTS: CONSTANT VELOCITY, VEHICLES (TRAIN TRACKS: 300K)



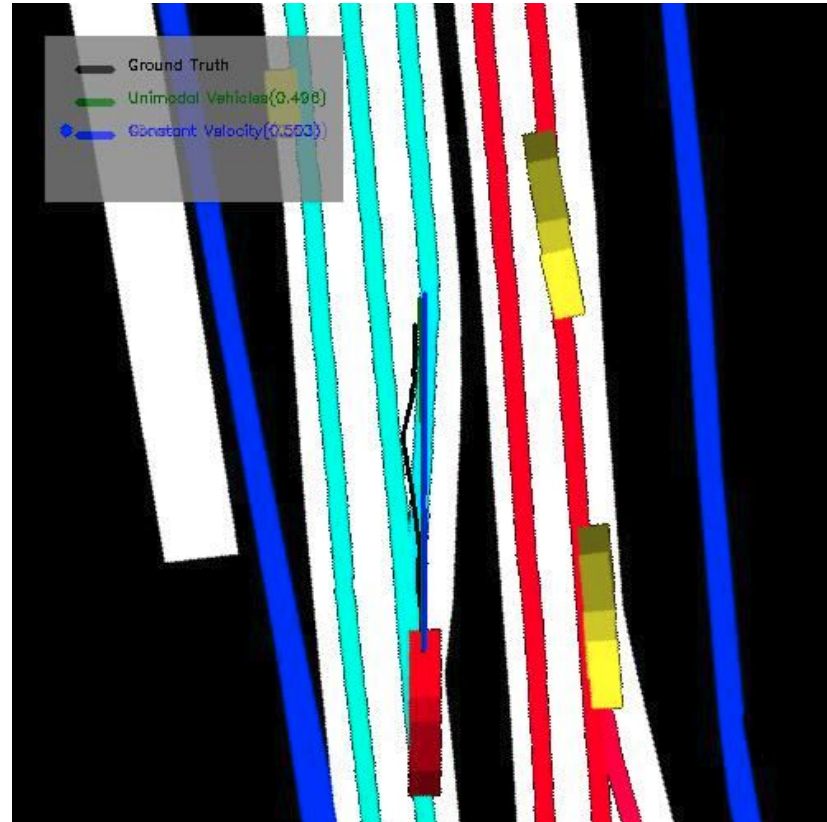
RESULTS (TRAIN TRACKS: 300K)

Unimodal > Constant Velocity
Predicted: Unimodal ✓



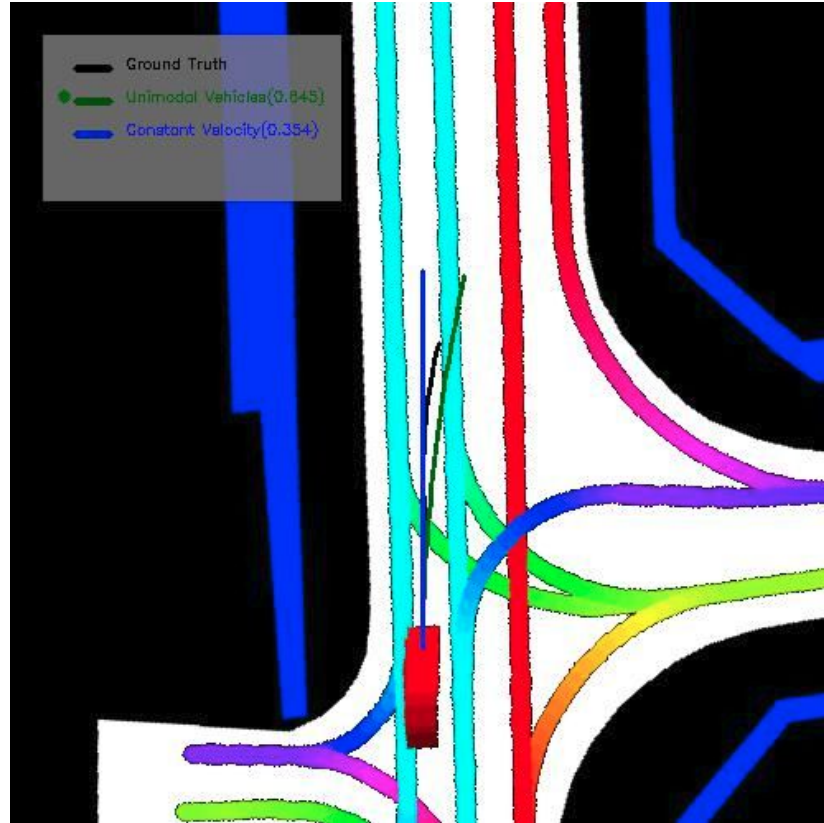
RESULTS (TRAIN TRACKS: 300K)

Constant Velocity > Unimodal
Predicted: Constant Velocity ✓

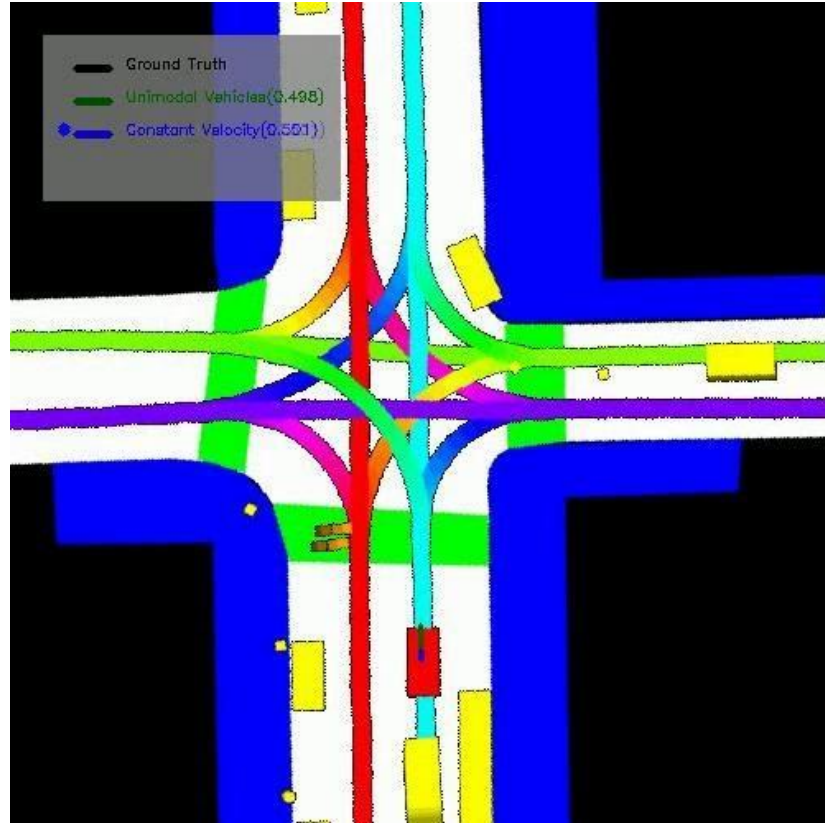


RESULTS (TRAIN TRACKS: 300K)

Constant Velocity > Unimodal
Predicted: Unimodal ✗



VISUALISATION (TRAIN TRACKS: 300K)



RESULTS (TRAIN TRACKS: 3MIL)

Unimodal > Constant Velocity
Predicted: Unimodal ✓

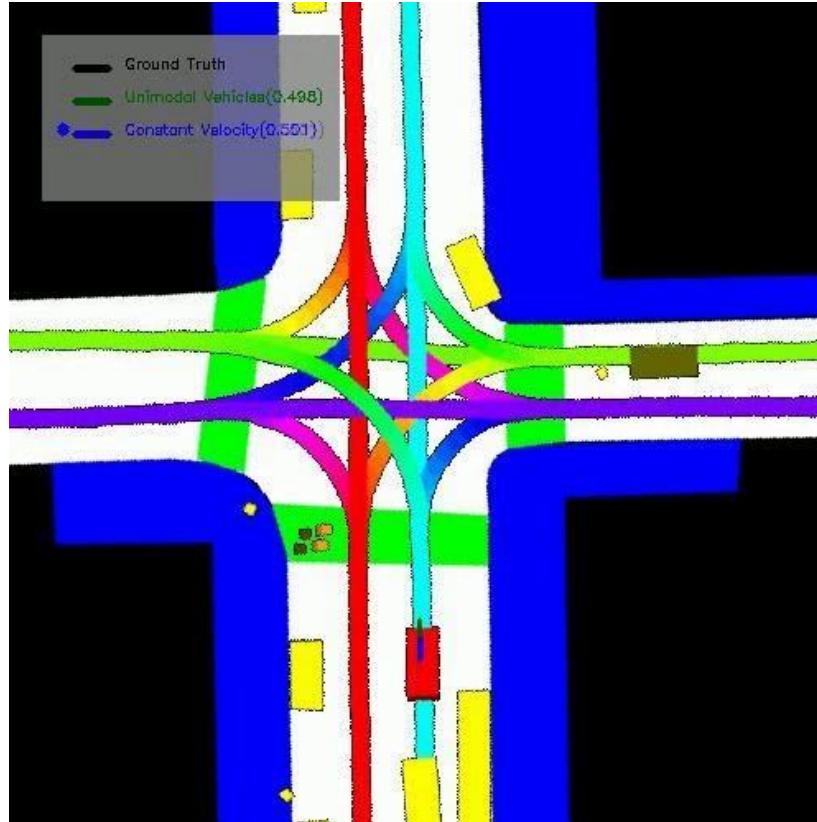


RESULTS (TRAIN TRACKS: 3MIL)

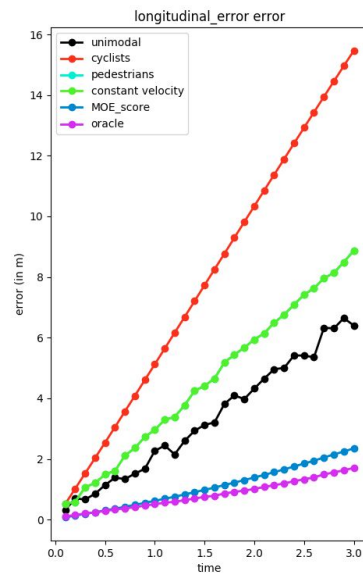
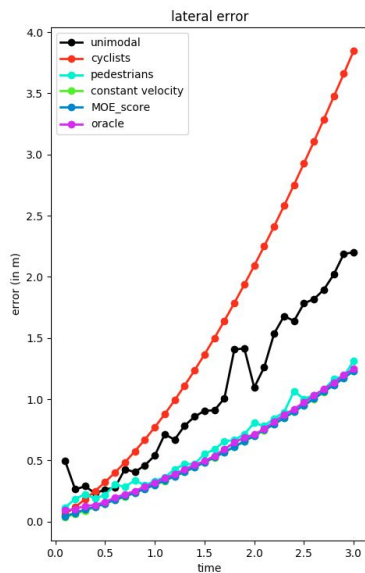
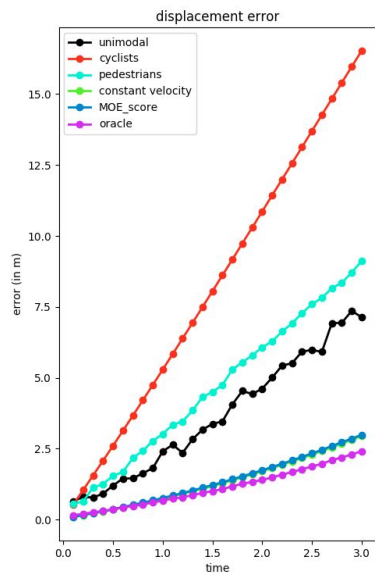
Constant Velocity > Unimodal
Predicted: Constant Velocity ✓



VISUALISATION (TRAIN TRACKS: 3MIL)

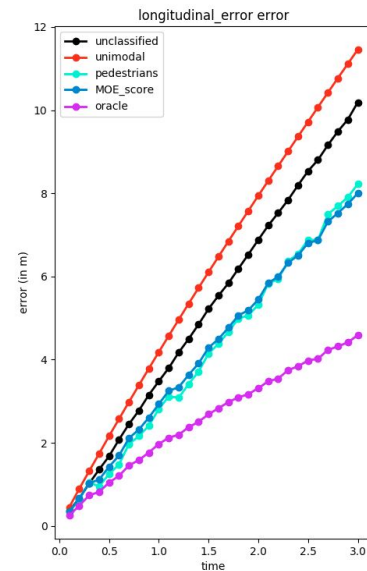
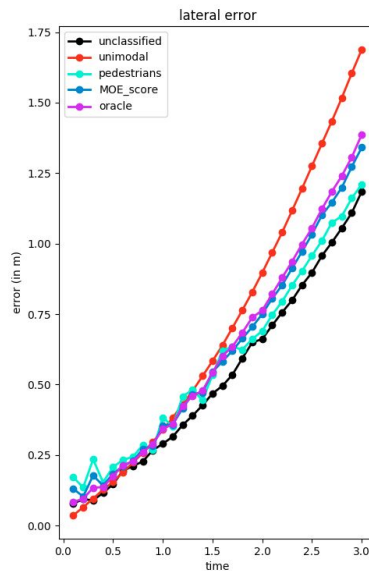
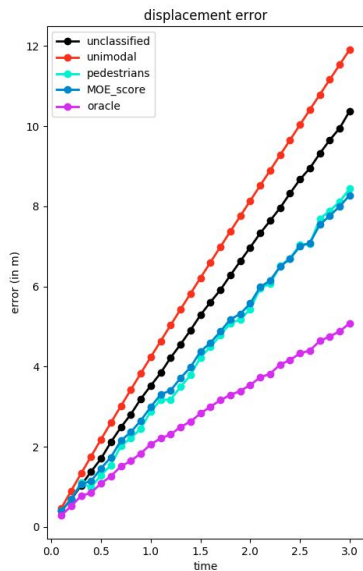


EXPERTS: VEHICLES, PEDESTRIAN, CYCLISTS, CONSTANT VELOCITY (TRAIN TRACKS: 5MIL)



Other experiments: 600k, 3 million

EXPERTS: VEHICLES, PEDESTRIAN, UNCLASSIFIED (TRAIN TRACKS: 6MIL)



CONCLUSION

- End-to-End Model does not provide improvement over Vehicles Model
- Frozen MoE Model (Experts: Constant Velocity, Unimodal Vehicles) does not provide improvement over Unimodal Vehicles model
- Frozen MoE Model (Experts: Unimodal Vehicles, Unimodal Pedestrians, Unimodal Unclassified) provides average score values similar to the Pedestrian Model, and better scores than the Unimodal Vehicles and Unimodal Unclassified Models (computed on all tracks)
- Future work:
 - Hyper-parameter optimisation
 - Distance function based on angle between trajectories instead of smooth L1
 - Different Architecture

IMPACT

- Mixture of experts model automatically chooses expert for each track
 - Eliminates the need to have different model for different types of tracks
- Created initial architecture for such an approach that can be used as a building block for further development

ACKNOWLEDGEMENT

- Corina (Advisor)
- Eric
- Freddy
- Tung Phan
- Sang Uk Lee

QUESTIONS?